

WHAT IS CLAIMED IS:

1. A method of mapping a set of  $n$ -dimensional input patterns to an  $m$ -dimensional space using locally defined neural networks, comprising the steps of:

- (a) creating a set of locally defined neural networks trained according to a mapping of a subset of the  $n$ -dimensional input patterns into an  $m$ -dimensional output space;
- (b) mapping additional  $n$ -dimensional input patterns using the locally defined neural networks.

2. The method of claim 1, wherein step (a) comprises the steps of:

- (i) selecting  $k$  patterns from the set of input patterns,  $\{\mathbf{x}_i, i = 1, 2, \dots k, \mathbf{x}_i \in \mathbb{R}^n\}$ ;
- (ii) mapping the patterns  $\{\mathbf{x}_i\}$  into an  $m$ -dimensional space ( $\mathbf{x}_i \rightarrow \mathbf{y}_i, i = 1, 2, \dots k, \mathbf{y}_i \in \mathbb{R}^m$ ), to form a training set  $T = \{(\mathbf{x}_i, \mathbf{y}_i), i = 1, 2, \dots k\}$ ;
- (iii) determining  $c$   $n$ -dimensional reference points,  $\{\mathbf{c}_i, i = 1, 2, \dots c, \mathbf{c}_i \in \mathbb{R}^n\}$ ;
- (iv) partitioning  $T$  into  $c$  disjoint clusters  $C_j$  based on a distance function  $d, \{C_j = \{(\mathbf{x}_i, \mathbf{y}_i): d(\mathbf{x}_i, \mathbf{c}_j) \leq d(\mathbf{x}_i, \mathbf{c}_k) \text{ for all } k \neq j; j = 1, 2, \dots c; i = 1, 2, \dots k\}$ ; and
- (v) training  $c$  independent local networks  $\{\text{Net}_i^L, i = 1, 2, \dots c\}$ , with the respective pattern subsets  $C_i$ .

3. The method of claim 2, wherein said step (iii) is performed using a clustering methodology.

4. The method of claim 2, wherein said step (b) comprises the steps of:

- (i) for an additional  $n$ -dimensional input pattern  $\mathbf{x} \in \mathbb{R}^n$ , determining the distance to each reference point in  $\{\mathbf{c}_i\}$ ;
- (ii) identifying the reference point  $\mathbf{c}_j$  closest to the input pattern  $\mathbf{x}$ ; and
- (iii) mapping  $\mathbf{x} \rightarrow \mathbf{y}$ ,  $\mathbf{y} \in \mathbb{R}^m$ , using the local neural network  $\text{Net}_j^L$  associated with the reference point  $\mathbf{c}_j$  identified in step (ii).

5. The method of claim 1, wherein step (a) comprises the steps of:

- (i) selecting  $k$  patterns of the set of  $n$ -dimensional input patterns,  $\{\mathbf{x}_i, i = 1, 2, \dots, k, \mathbf{x}_i \in \mathbb{R}^n\}$ ;
- (ii) mapping the patterns  $\{\mathbf{x}_i\}$  into an  $m$ -dimensional space ( $\mathbf{x}_i \rightarrow \mathbf{y}_i, i = 1, 2, \dots, k, \mathbf{y}_i \in \mathbb{R}^m$ ), to form a training set  $T = \{(\mathbf{x}_i, \mathbf{y}_i), i = 1, 2, \dots, k\}$ ;
- (iii) determining  $c$   $m$ -dimensional reference points,  $\{\mathbf{c}_i, i = 1, 2, \dots, c, \mathbf{c}_i \in \mathbb{R}^m\}$ ;
- (iv) partitioning  $T$  into  $c$  disjoint clusters  $C_j$  based on a distance function  $d$ ,  $\{C_j = \{(\mathbf{x}_i, \mathbf{y}_i): d(\mathbf{y}_i, \mathbf{c}_j) \leq d(\mathbf{y}_i, \mathbf{c}_k) \text{ for all } k \neq j; j = 1, 2, \dots, c; i = 1, 2, \dots, k\}\}$ ;
- (v) training  $c$  independent local networks  $\{\text{Net}_i^L, i = 1, 2, \dots, c\}$ , with the respective pattern subsets  $C_i$ ; and
- (vi) training a global network  $\text{Net}^G$  using all the patterns in  $T$ .

6. The method of claim 5, wherein said step (iii) is performed using a clustering methodology.

7. The method of claim 5, wherein step (b) comprises the steps of:

- (i) for an additional  $n$ -dimensional pattern  $\mathbf{x} \in \mathbb{R}^n$ , mapping  $\mathbf{x} \rightarrow \mathbf{y}', \mathbf{y}' \in \mathbb{R}^m$ , using  $\text{Net}^G$ ;

- (ii) determining the distance of  $\mathbf{y}'$  to each reference point in  $\{\mathbf{c}_i\}$ ;
- (iii) identifying the reference point  $\mathbf{c}_j$  closest to  $\mathbf{y}'$ , and
- (iv) mapping  $\mathbf{x} \rightarrow \mathbf{y}$ ,  $\mathbf{y} \in \mathbb{R}^m$ , using the local neural network  $\text{Net}_j^L$  associated with the reference point  $\mathbf{c}_j$  identified in step (iii).

8. A computer program product comprising a computer usable medium having computer readable program code means embodied in said medium for causing an application program to execute on a computer that maps a set of  $n$ -dimensional input patterns to an  $m$ -dimensional space using locally defined neural networks, said computer readable program code means comprising:

a first computer readable program code means for causing the computer to create a set of locally defined neural networks trained according to a mapping of a subset of the  $n$ -dimensional input patterns into an  $m$ -dimensional space;

a second computer readable program code means for causing the computer to project additional  $n$ -dimensional patterns of the input set using the locally defined neural networks.

9. The computer program product of claim 8, wherein said first computer readable code means comprises:

- (i) computer readable program code means for selecting  $k$  patterns from the set of input patterns,  $\{\mathbf{x}_i, i = 1, 2, \dots, k, \mathbf{x}_i \in \mathbb{R}^n\}$ ;
- (ii) computer readable program code means for mapping the patterns  $\{\mathbf{x}_i\}$  into an  $m$ -dimensional space  $(\mathbf{x}_i \rightarrow \mathbf{y}_i, i = 1, 2, \dots, k, \mathbf{y}_i \in \mathbb{R}^m)$ , to form a training set  $T = \{(\mathbf{x}_i, \mathbf{y}_i), i = 1, 2, \dots, k\}$ ;

(iii) computer readable program code means for determining  $c$   $n$ -dimensional reference points,  $\{\mathbf{c}_i, i = 1, 2, \dots, c, \mathbf{c}_i \in \mathbb{R}^n\}$ ;

(iv) computer readable program code means for partitioning  $T$  into  $c$  disjoint clusters  $C_j$  based on a distance function  $d$ ,  $\{C_j = \{(\mathbf{x}_i, \mathbf{y}_i) : d(\mathbf{x}_i, \mathbf{c}_j) \leq d(\mathbf{x}_i, \mathbf{c}_k) \text{ for all } k \neq j; j = 1, 2, \dots, c; i = 1, 2, \dots, k\}\}$ ; and

(v) computer readable program code means for training  $c$  independent local networks  $\{\text{Net}_i^L, i = 1, 2, \dots, c\}$ , with the respective pattern subsets  $C_i$ .

10. The computer program product of claim 9, wherein said computer readable program code means uses a clustering methodology.

11. The computer program product of claim 9, wherein said second computer readable code means comprises:

(i) for an additional  $n$ -dimensional pattern  $\mathbf{x} \in \mathbb{R}^n$ , computer readable program code means for determining the distance to each reference point in  $\{\mathbf{c}_i\}$ ;

(ii) computer readable program code means for identifying the reference point  $\mathbf{c}_j$  closest to the input pattern  $\mathbf{x}$ ; and

(iii) computer readable program code means for mapping  $\mathbf{x} \rightarrow \mathbf{y}, \mathbf{y} \in \mathbb{R}^m$ , using the local neural network  $\text{Net}_j^L$  associated with the reference point  $\mathbf{c}_j$  identified in step (ii).

12. The computer program product of claim 8, wherein said first computer readable program code means comprises:

(i) computer readable program code means for selecting  $k$  patterns of the set of  $n$ -dimensional input patterns,  $\{\mathbf{x}_i, i = 1, 2, \dots, k, \mathbf{x}_i \in \mathbb{R}^n\}$ ;

(ii) computer readable program code means for mapping the patterns  $\{\mathbf{x}_i\}$  into an  $m$ -dimensional space ( $\mathbf{x}_i \rightarrow \mathbf{y}_i$ ,  $i = 1, 2, \dots k$ ), to form a training set  $T = \{(\mathbf{x}_i, \mathbf{y}_i), i = 1, 2, \dots k\}$ ;

(iii) computer readable program code means for determining  $c$   $m$ -dimensional reference points,  $\{\mathbf{c}_i, i = 1, 2, \dots c, \mathbf{c}_i \in \mathbb{R}^m\}$ ;

(iv) computer readable program code means for partitioning  $T$  into  $c$  disjoint clusters  $C_j$  based on a distance function  $d$ ,  $\{C_j = \{(\mathbf{x}_i, \mathbf{y}_i): d(\mathbf{y}_i, \mathbf{c}_j) \leq d(\mathbf{y}_i, \mathbf{c}_k) \text{ for all } k \neq j; j = 1, 2, \dots c; i = 1, 2, \dots k\}\}$ ;

(v) computer readable program code means for training  $c$  independent local networks  $\{\text{Net}_i^L, i = 1, 2, \dots c\}$ , with the respective pattern subsets  $C_i$ ; and

(vi) computer readable program code means for training a global network  $\text{Net}^G$  using all the patterns in  $T$ .

13. The computer program product of claim 12, wherein said computer readable program code means uses a clustering methodology.

14. The computer program product of claim 12, wherein said second computer readable program code means comprises:

(i) for an additional  $n$ -dimensional pattern  $\mathbf{x} \in \mathbb{R}^n$ , computer readable program code means for mapping  $\mathbf{x} \rightarrow \mathbf{y}'$ ,  $\mathbf{y}' \in \mathbb{R}^m$ , using  $\text{Net}^G$ ;

(ii) computer readable program code means for determining the distance of  $\mathbf{y}'$  to each reference point in  $\{\mathbf{c}_i\}$ ;

(iii) computer readable program code means for identifying the reference point  $\mathbf{c}_j$  closest to  $\mathbf{y}'$ , and

(iv) computer readable program code means for mapping  $\mathbf{x} \rightarrow \mathbf{y}$ ,  $\mathbf{y} \in \mathbb{R}^m$ , using the local neural network  $\text{Net}_j^L$  associated with the reference point  $\mathbf{c}_j$  identified in step (iii).